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# Learning programs with magic values

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# Motivation

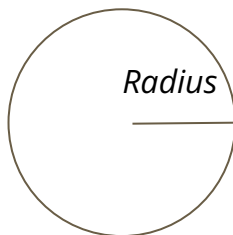
A *magic value* is a constant symbol in a program which has no clear explanation for its choice: it *magically* works.

Positive examples	Negative examples
[a,e,6,7,q,2]	[6,e,a,2,q,6,e]
[p,3,9,y,5,r,a,q,7]	[u,k,a,b,c,z,r,t,5,e,t]

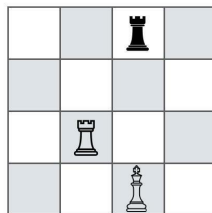
$$f(A) \leftarrow \text{head}(A, \mathbf{7})$$
$$f(A) \leftarrow \text{tail}(A, B), f(B)$$

# Motivation

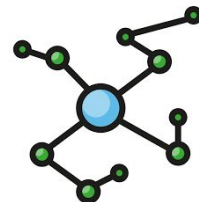
```
area(Radius,Area) ←  
  square(Radius,SqRadius),  
  mult(SqRadius, 3.14, Area).
```



```
rookprotected(State) ←  
  piece(State1,Piece1,white,rook),  
  piece(State,Piece2,white,king),  
  distance(Piece1,Piece2,1).
```



```
drug(Drug) ←  
  atom(Drug,Atom1),  
  atom(Drug,Atom2),  
  atomtype(Atom1,oxygen),  
  atomtype(Atom2,hydrogen),  
  distance(Atom1,Atom2,0.53)
```



# Existing approaches

Bottom clause (Progol, Aleph):

- bottom clause can grow large
- limited recursion and lack of predicate invention

# Existing approaches

Precompute every possible rule in the hypothesis space (ASPAL, ILASP, HEXMIL, ProSynth)

H1:  $f(A) \leftarrow \text{head}(A, 1)$

H2:  $f(A) \leftarrow \text{head}(A, 2)$

H3:  $f(A) \leftarrow \text{head}(A, 3)$

H4:  $f(A) \leftarrow \text{head}(A, 4)$

H5:  $f(A) \leftarrow \text{head}(A, 5)$

H6:  $f(A) \leftarrow \text{head}(A, 6)$

...

# Existing approaches

Unary predicate symbols, one for each constant symbol (Popper,  $\delta$ ILP)

H1:  $f(A) \leftarrow \text{head}(A,B), c1(B)$

H2:  $f(A) \leftarrow \text{head}(A,B), c2(B)$

H3:  $f(A) \leftarrow \text{head}(A,B), c3(B)$

H4:  $f(A) \leftarrow \text{head}(A,B), c4(B)$

H5:  $f(A) \leftarrow \text{head}(A,B), c5(B)$

H6:  $f(A) \leftarrow \text{head}(A,B), c6(B)$

...

# Existing approaches: limitations

Enumeration of constant symbols

- cannot scale to large or infinite domains
- suffer from performance issue

# Our approach

Existing approaches		Our approach
$f(List) \leftarrow head(List, 1).$	$f(List) \leftarrow head(List, E), c1(E).$	$f(A) \leftarrow head(List, \mathbf{E}),$ $@magic(\mathbf{E}).$
$f(List) \leftarrow head(List, 2).$	$f(List) \leftarrow head(List, E), c2(E).$	
$f(List) \leftarrow head(List, 3).$	$f(List) \leftarrow head(List, E), c3(E).$	
$f(List) \leftarrow head(List, 4).$	$f(List) \leftarrow head(List, E), c4(E).$	
$f(List) \leftarrow head(List, 5).$	$f(List) \leftarrow head(List, E), c5(E).$	
$f(List) \leftarrow head(List, 6).$	$f(List) \leftarrow head(List, E), c6(E).$	
..	...	

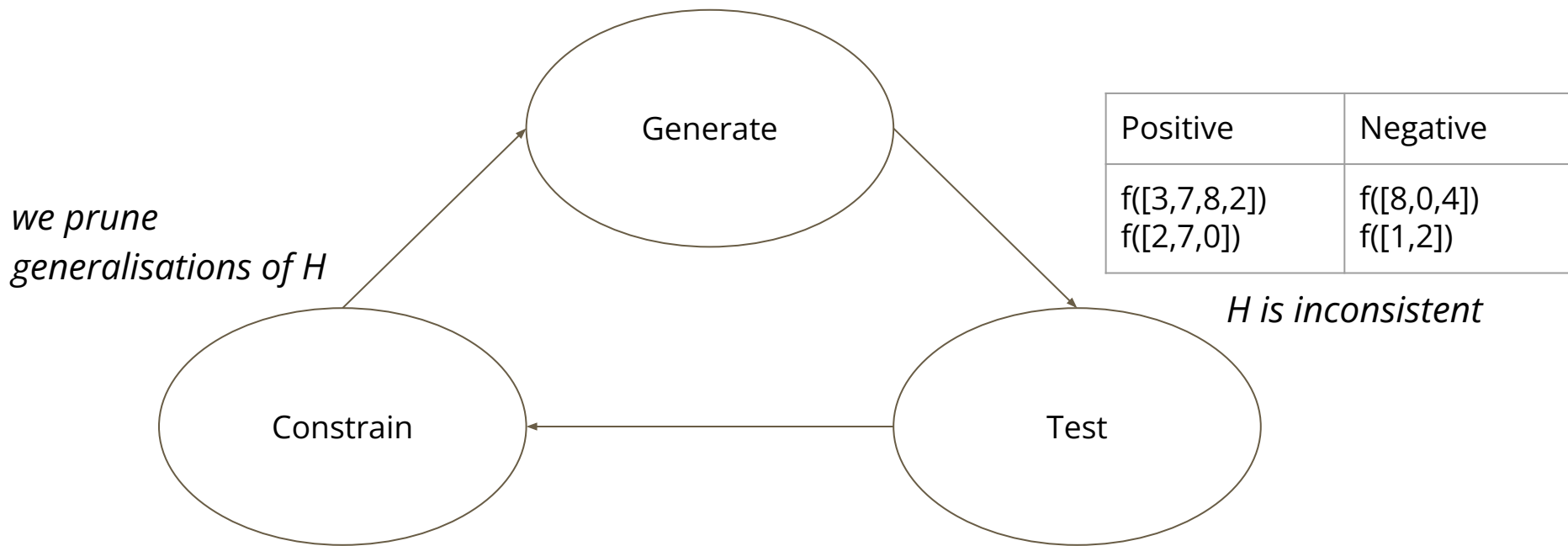
# Related Work

Our approach is inspired by Aleph's lazy evaluation procedure:

- can learn constants from reasoning from multiple examples
- limited learning of recursion and lack of predicate invention
- requires strong user bias

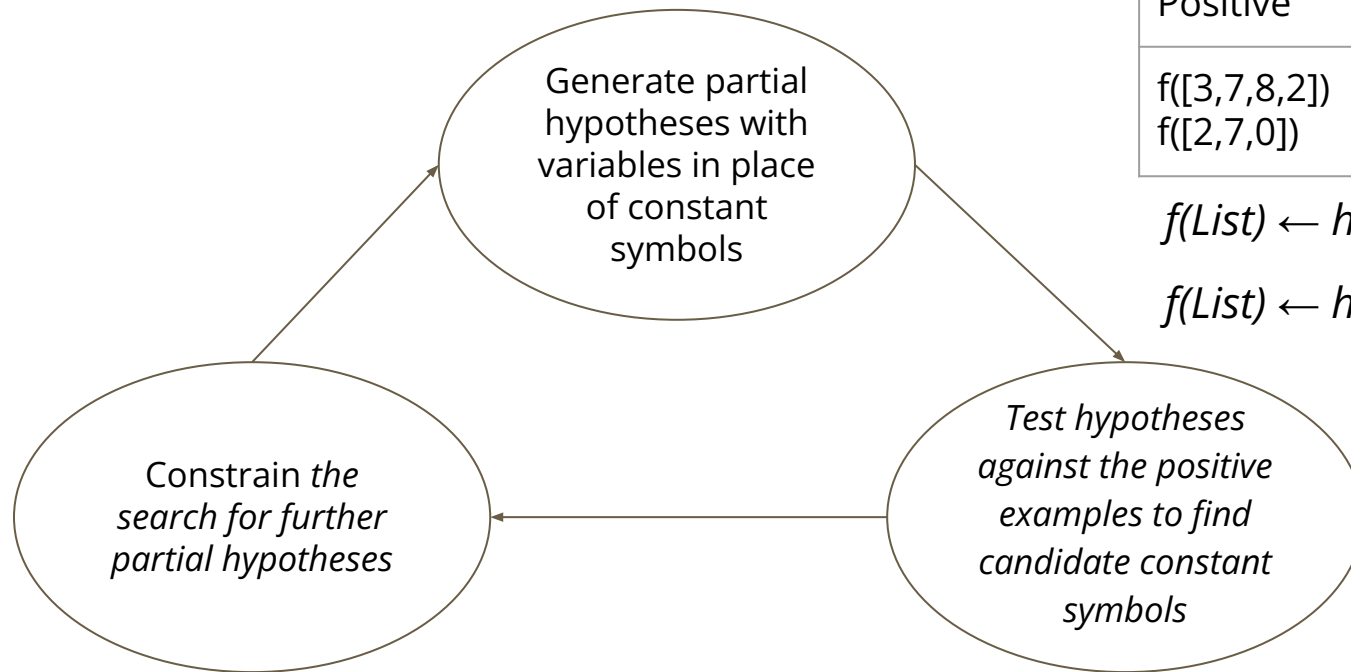
# Learning From Failures

$H : f(List) \leftarrow head(List, E), c1(E).$



# Our approach

$H : f(List) \leftarrow head(List, E), @magic(E)$



Positive	Negative
$f([3,7,8,2])$ $f([2,7,0])$	$f([8,0,4])$ $f([1,2])$

$f(List) \leftarrow head(List, 3).$

$f(List) \leftarrow head(List, 2).$

# Implementation

We implement our approach in MagicPopper

Based on the LFF learner Popper

# Experiments

Q1: How well does MagicPopper perform compared to other approaches?

# Q1: comparison with other approaches

Task	Aleph	Metagol	Popper	MagicPopper
<i>md</i>	<b>100 ± 0</b>	50 ± 0	<b>100 ± 0</b>	<b>100 ± 0</b>
<i>buttons-next</i>	81 ± 0	50 ± 0	<b>100 ± 0</b>	<b>100 ± 0</b>
<i>coins-next</i>	50 ± 0	50 ± 0	<b>100 ± 0</b>	<b>100 ± 0</b>
<i>buttons-goal</i>	<b>100 ± 0</b>	50 ± 0	98 ± 1	<b>100 ± 0</b>
<i>coins-goal</i>	50 ± 0	50 ± 0	<b>100 ± 0</b>	<b>100 ± 0</b>
<i>gt-centipede-goal</i>	<b>99 ± 0</b>	50 ± 0	75 ± 0	75 ± 0
<i>gt-centipede-legal</i>	<b>100 ± 0</b>	50 ± 0	<b>100 ± 0</b>	<b>100 ± 0</b>
<i>gt-centipede-next</i>	<b>100 ± 0</b>	50 ± 0	<b>100 ± 0</b>	<b>100 ± 0</b>
<i>krk</i>	<b>100 ± 0</b>	54 ± 4	96 ± 1	99 ± 0
<i>list</i>	50 ± 0	<b>100 ± 0</b>	49 ± 0	<b>100 ± 0</b>
<i>powerof2</i>	86 ± 1	58 ± 5	84 ± 1	<b>100 ± 0</b>
<i>append</i>	95 ± 1	<b>99 ± 0</b>	96 ± 1	96 ± 1

**Predictive accuracies**

# Q1: comparison with other approaches

Task	Aleph	Metagol	Popper	MagicPopper
<i>md</i>	<b>0 ± 0</b>		1 ± 0	<b>0 ± 0</b>
<i>buttons-next</i>	32 ± 1		<b>3 ± 0</b>	4 ± 0
<i>coins-next</i>			<b>53 ± 0</b>	99 ± 1
<i>buttons-goal</i>	<b>0 ± 0</b>		1 ± 0	<b>0 ± 0</b>
<i>coins-goal</i>			<b>0 ± 0</b>	<b>0 ± 0</b>
<i>gt-centipede-goal</i>	<b>0 ± 0</b>		23 ± 0	6 ± 0
<i>gt-centipede-legal</i>	<b>0 ± 0</b>		4 ± 0	1 ± 0
<i>gt-centipede-next</i>	<b>0 ± 0</b>		10 ± 0	<b>0 ± 0</b>
<i>krk</i>	<b>0 ± 0</b>		35 ± 6	6 ± 0
<i>list</i>		36 ± 8		<b>2 ± 0</b>
<i>powerof2</i>	<b>0 ± 0</b>		18 ± 0	<b>0 ± 0</b>
<i>append</i>	1 ± 0	<b>0 ± 0</b>	298 ± 49	<b>0 ± 0</b>

Learning times

## Q1: comparison with other approaches

- **MagicPopper can outperform existing approaches in terms of learning times and predictive accuracies**

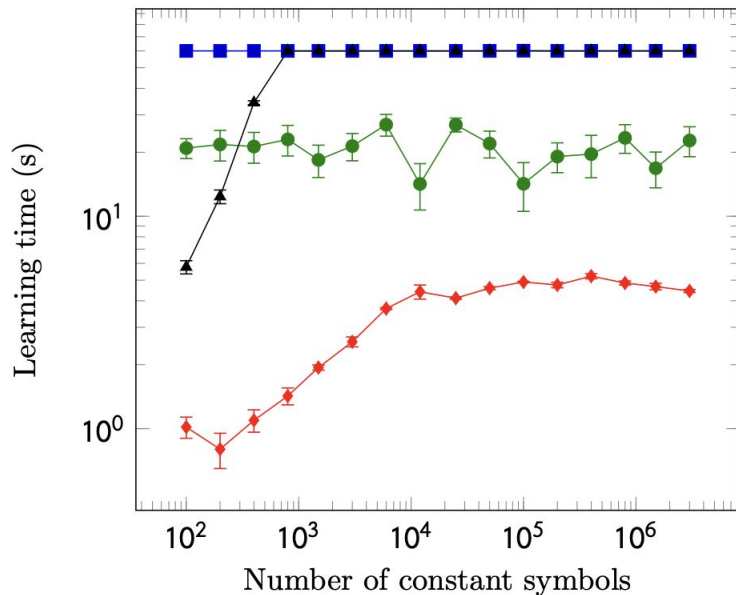
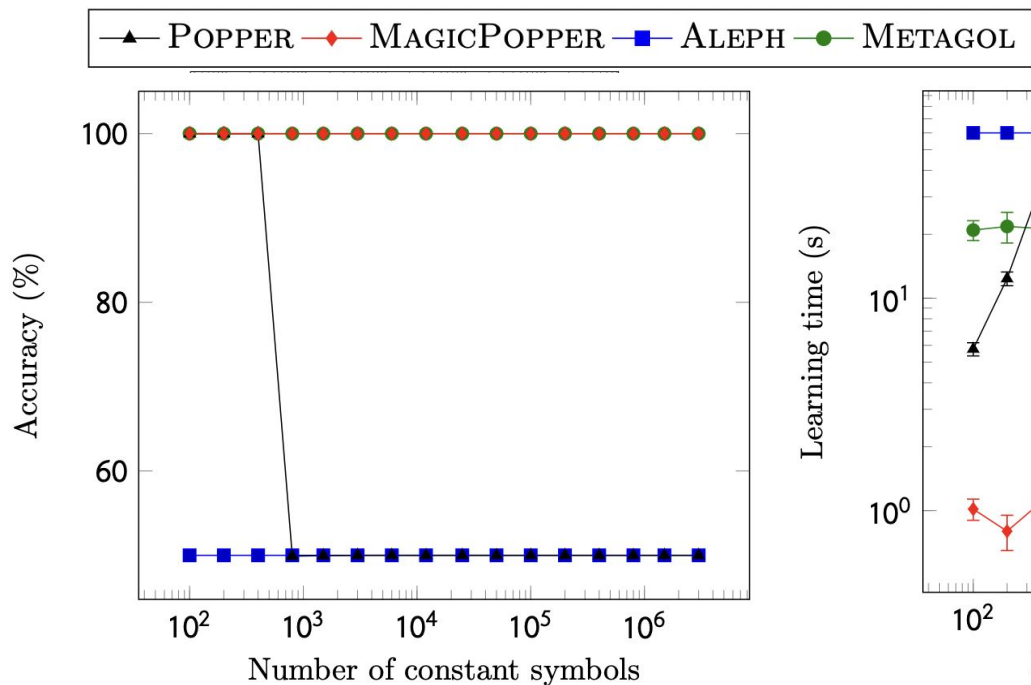
# Experiments

Q2: How well does MagicPopper scale with the number of constant symbols?

## Q2: scalability with respect to the number of constant symbols

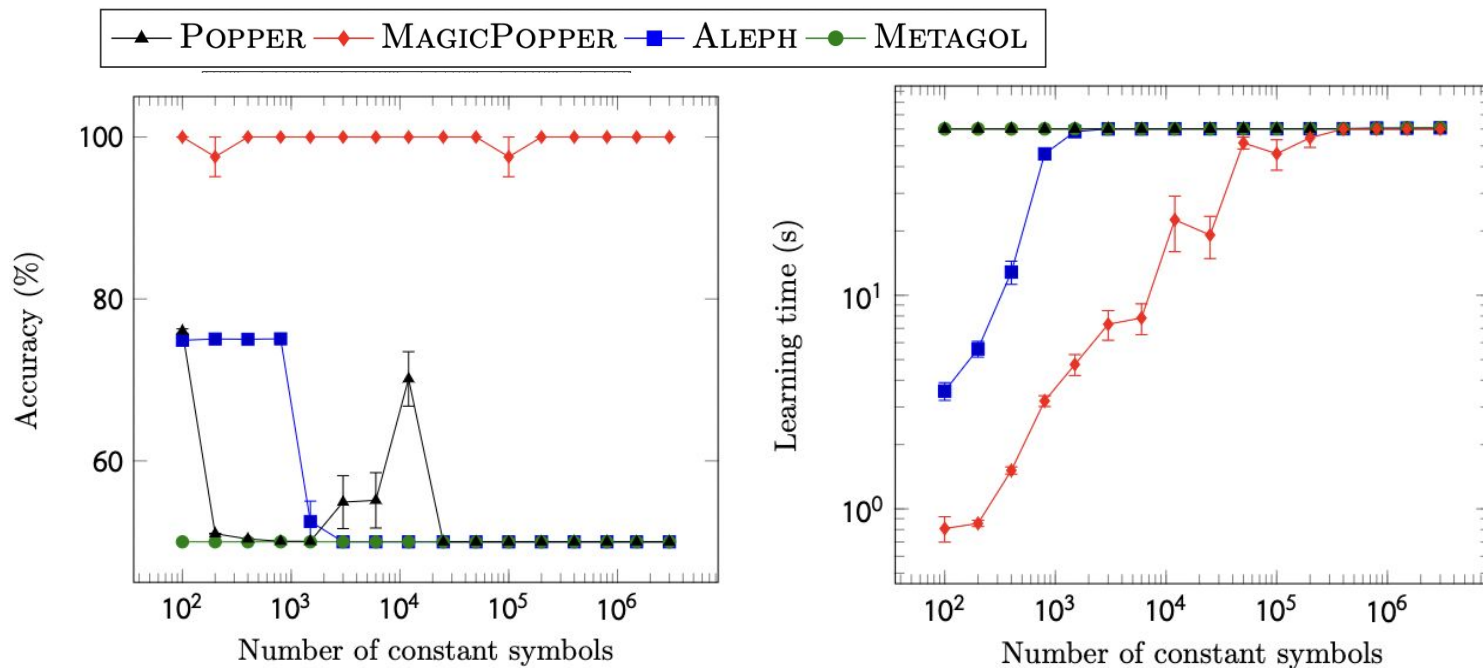
$f(A) \leftarrow \text{head}(A, 7)$

$f(A) \leftarrow \text{tail}(A, B), f(B)$



## Q2: scalability with respect to the number of constant symbols

$next\_val(A,5) \leftarrow does(A, \mathbf{player}, \mathbf{press\_button})$   
 $next\_val(A,B) \leftarrow does(A, \mathbf{player}, \mathbf{noop}), true\_val(A,C), succ(B,C)$



## Q2: scalability with respect to the number of constant symbols

- **MagicPopper can scale well with the number of constant symbols, up to millions**

# Experiments

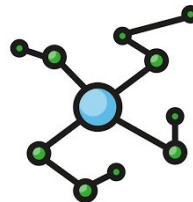
Q3: Can MagicPopper learn in infinite domains?

## Q3: learning in infinite domains

Task	Aleph	Metagol	Popper	MagicPopper
<i>pi</i>	<b>100 <math>\pm</math> 0</b>	50 $\pm$ 0	50 $\pm$ 0	99 $\pm$ 0
<i>equilibrium</i>	<b>100 <math>\pm</math> 0</b>	50 $\pm$ 0	62 $\pm$ 1	86 $\pm$ 7
<i>drug design</i>	63 $\pm$ 7	50 $\pm$ 0	50 $\pm$ 0	<b>98 <math>\pm</math> 0</b>
<i>next</i>	50 $\pm$ 0	50 $\pm$ 0	49 $\pm$ 0	<b>100 <math>\pm</math> 0</b>
<i>sumk</i>	50 $\pm$ 0	50 $\pm$ 0	50 $\pm$ 0	<b>100 <math>\pm</math> 0</b>

### Predictive accuracies

```
drug(Drug) ←  
  atom(Drug,Atom1),  
  atom(Drug,Atom2),  
  atomtype(Atom1,oxygen),  
  atomtype(Atom2,hydrogen),  
  distance(Atom1,Atom2,0.53)
```

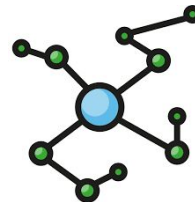


## Q3: learning in infinite domains

Task	Aleph	Metagol	Popper	MagicPopper
<i>pi</i>	4 ± 1			1 ± 0
<i>equilibrium</i>	0 ± 0			72 ± 17
<i>drug design</i>				6 ± 3
<i>next</i>				25 ± 0
<i>sumk</i>				99 ± 1

### Learning times

```
drug(Drug) ←  
  atom(Drug,Atom1),  
  atom(Drug,Atom2),  
  atomtype(Atom1,oxygen),  
  atomtype(Atom2,hydrogen),  
  distance(Atom1,Atom2,0.53)
```



## Q3: learning in infinite domains

- **MagicPopper can learn in infinite domains**

# Conclusion

MagicPopper, approach to learn programs with magic values. It can:

- outperform state-of-the art approaches,
- scale to domains with millions of constant symbols,
- learn in continuous domains,
- learn optimal programs and recursive programs.

# Future Work and Limitations

- Noise: identify magic values from noisy examples
- Numerical reasoning from multiple examples (eg identify thresholds)

# References

- Corapi, D., Russo, A., Lupu, E.: Inductive logic programming in answer set programming. In: Inductive Logic Programming - 21st International Conference, (2011).
- Law, M., Russo, A., Broda, K.: The ILASP system for learning Answer Set Programs. [www.ilasp.com](http://www.ilasp.com) (2015).
- Kaminski, T., Eiter, T., Inoue, K.: Exploiting answer set programming with external sources for meta-interpretive learning. *Theory and Practice of Logic Programming* 18(3-4), (2018).
- Raghothaman, M., Mendelson, J., Zhao, D., Naik, M., Scholz, B.: Provenance-guided synthesis of datalog programs. *Proceedings of the ACM on Programming Languages* 4(POPL), (2019).
- Cropper, A., Morel, R.: Learning programs by learning from failures. *Machine Learning* 110(4), 801–856 (2021).
- Evans, R., Grefenstette, E.: Learning explanatory rules from noisy data. *Journal of Artificial Intelligence Research* 61, (2018).
- Srinivasan, A.: The ALEPH manual. *Machine Learning at the Computing Laboratory* (2001).
- Srinivasan, A., Camacho, R.: Numerical reasoning with an ILP system capable of lazy evaluation and customised search. *The Journal of Logic Programming* 40(2), 185–213 (1999).
- Muggleton, S.H., Lin, D., Pahlavi, N., Tamaddoni-Nezhad, A.: Meta- interpretive learning: application to grammatical inference. *Machine Learning* 94, (2014).

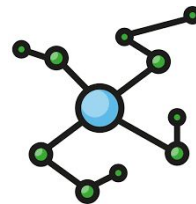
# Tasks

```
equilibrium(Object) ←  
  forces(Object, Forces),  
  sum(Forces, Sum), mass(Object, Mass),  
  mult(Mass, 9.81, Sum).
```



```
next(A, q) ← my true(A, q), does(A, robot, a)  
next(A, p) ← my true(A, q), does(A, robot, b)  
next(A, q) ← my true(A, r), does(A, robot, c)  
next(A, r) ← my true(A, r), does(A, robot, a)  
next(A, r) ← my true(A, r), does(A, robot, b)  
next(A, q) ← my true(A, p), does(A, robot, b)  
next(A, p) ← my true(A, p), does(A, robot, c)  
next(A, B) ← my true(A, C), my succ(C, B)  
next(A, p) ← not my true(A, B), does(A, robot, a)
```

```
drug(Drug) ←  
  atom(Drug, Atom1),  
  atom(Drug, Atom2),  
  atomtype(Atom1, oxygen),  
  atomtype(Atom2, hydrogen),  
  distance(Atom1, Atom2, 0.53)
```



```
next(A, B) ← head(A, 4.543), tail(A, C), head(C, B).  
next(A, B) ← tail(A, C), next(C, B).
```

```
sumk(A) ← member(A, B), member(A, C), add(B, C, 612)
```

# Implementation: Bias

Predicate	Type
head_pred(f,1)	(state)
body_pred(cell,4)	(state,pos,color,type)
body_pred(distance,3)	(pos,pos,int)

Setting	Bias	Example
Arguments	cell 3 distance 3	$f(\text{State}) \leftarrow \text{cell}(\text{State}, \text{Piece1}, \mathbf{Color1}, \text{Type}), \text{cell}(\text{State}, \text{Piece2}, \mathbf{Color2}, \text{Type}), \text{distance}(\text{Piece1}, \text{Piece2}, \mathbf{Dist})$
Types	integer type	$f(\text{State}) \leftarrow \text{cell}(\text{State}, \text{Piece1}, \text{Color}, \mathbf{Type1}), \text{cell}(\text{State}, \text{Piece2}, \text{Color}, \mathbf{Type2}), \text{distance}(\text{Piece1}, \text{Piece2}, \mathbf{Dist})$
All		$f(\text{State}) \leftarrow \text{cell}(\mathbf{State}, \mathbf{Piece1}, \mathbf{Color1}, \mathbf{Type1}), \text{cell}(\mathbf{State}, \mathbf{Piece2}, \mathbf{Color2}, \mathbf{Type2}), \text{distance}(\mathbf{Piece1}, \mathbf{Piece2}, \mathbf{Dist})$