

Learning big logical rules by joining small rules

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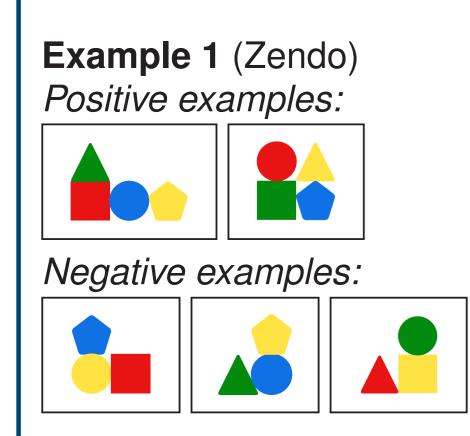
1 - Introduction

UK Research

and Innovation

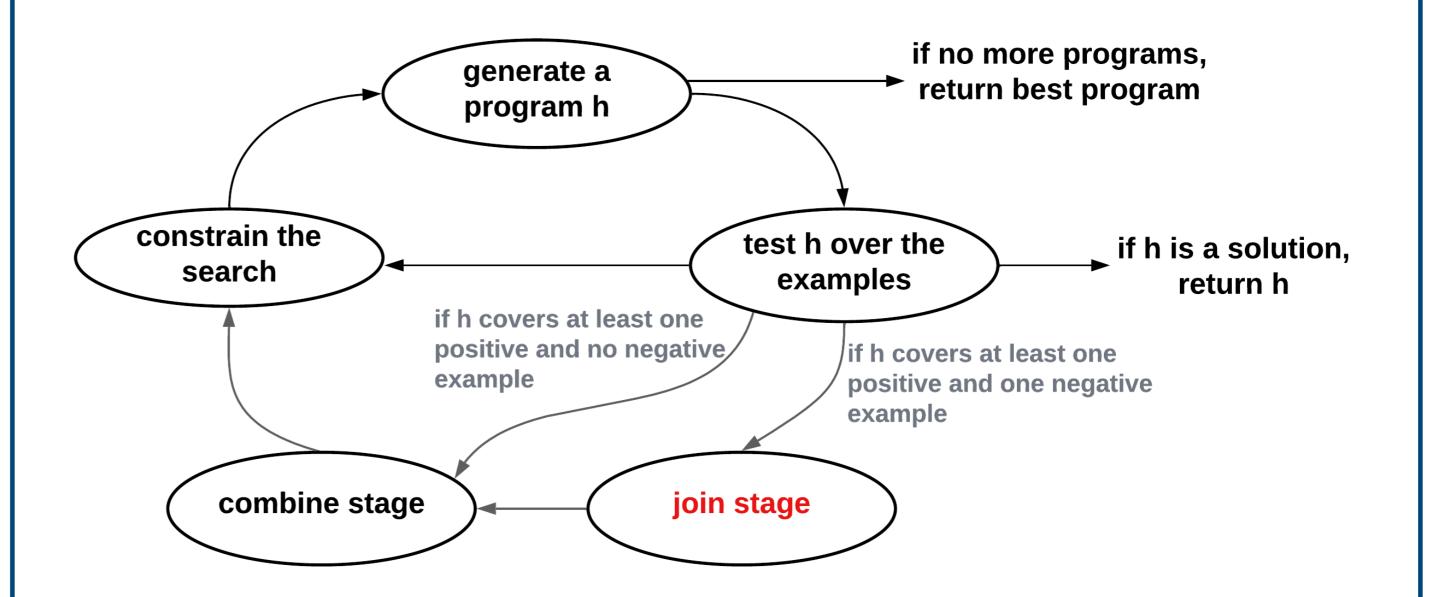
The goal of inductive logic programming (ILP) is to induce a program (a set of logical rules) that generalises training examples.

Problem: learning programs with big rules is difficult.



2 - Our approach (JOINER)

Key idea: learn small programs independently and then try to find conjunctions of these programs which cover no negative examples.



 $zendo(S) \leftarrow piece(S,B), blue(B),$ piece(S,R), red(R),piece(S,G), green(G)

We introduce an approach where we join small rules to learn big rules.

We first search for rules that entail at least one positive example, such as:

 $\begin{array}{l} \text{zendo}_1(S) \leftarrow \text{piece}(S,B), \, \text{blue}(B) \\ \text{zendo}_2(S) \leftarrow \text{piece}(S,R), \, \text{red}(R) \\ \text{zendo}_3(S) \leftarrow \text{piece}(S,G), \, \text{green}(G) \\ \text{zendo}_4(S) \leftarrow \text{piece}(S,Y), \, \text{yellow}(Y) \end{array}$

We then search for subsets of these rules which entail at least one positive example and no negative examples:

 $\begin{array}{l} \text{zendo}(S) \leftarrow \text{zendo}_1(S), \, \text{zendo}_2(S) \\ \text{zendo}_3(S) \end{array}$

Example 2 (List classification)PositiveNegativef([a,b,c,d])f([a,c,d,e])f([c,b,d,e])f([c,b])f([c,b,d,e])f([c,b])We first learn programs that errors

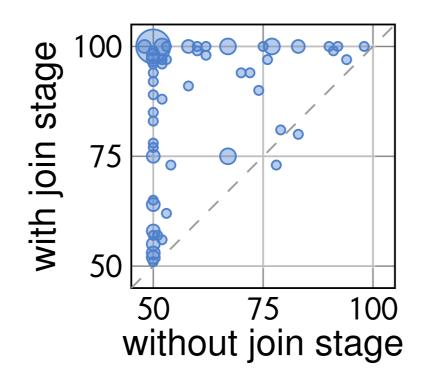
We first learn programs that entail at least one positive example:

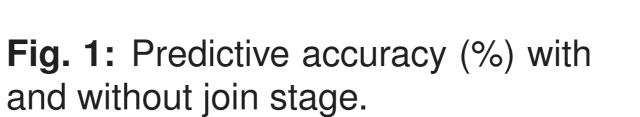
{	$f_1(List) \leftarrow head(List,a) \}$
ł	$f_2(List) \leftarrow head(List,c) $
>	$f_2(l \text{ ist}) \leftarrow tail(l \text{ ist Tail}) head(Tail h$

We develop a Boolean satisfiability approach to find conjunctions in the join stage.

4 - Experiment

- Q1 Can the join stage improve learning performance?
- Q2 How well does JOINER scale with the size of rules?
- Q3 How well does JOINER compare against other approaches?





Task	ALEPH	Сомво	JOINER
iggp	78 ± 3	86 ± 2	$\begin{array}{r} \textbf{96} \pm \textbf{1} \\ \textbf{94} \pm \textbf{2} \\ \textbf{98} \pm \textbf{1} \\ \textbf{100} \pm \textbf{0} \\ \textbf{100} \pm \textbf{0} \\ \textbf{89} \pm \textbf{1} \end{array}$
zendo	100 ± 0	86 ± 3	
pharma	50 ± 0	53 ± 2	
imdb	67 ± 6	100 \pm 0	
string	50 ± 0	50 ± 0	
onedarc	51 ± 1	57 ± 2	

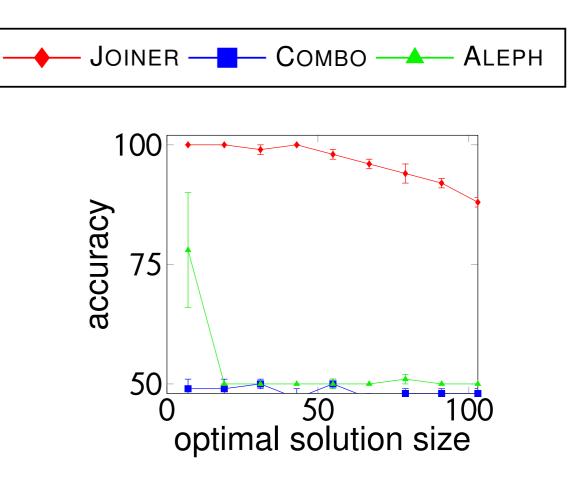


Fig. 2: Predictive accuracy versus the size of programs for *zendo*.

- Q1 The join stage can substantially improve predictive accuracies.
- Q2 JOINER can learn rules with

 $\{ \begin{array}{l} T_3(\text{LISt}) \leftarrow \text{tail}(\text{List},\text{Tail}),\text{head}(\text{Tail},\text{b}) \\ f_4(\text{List}) \leftarrow \text{head}(\text{List},\text{c}) \\ f_4(\text{List}) \leftarrow \text{tail}(\text{List},\text{Tail}), f_4(\text{Tail}) \\ f_5(\text{List}) \leftarrow \text{head}(\text{List},\text{d}) \\ f_5(\text{List}) \leftarrow \text{tail}(\text{List},\text{Tail}), f_5(\text{Tail}) \\ \end{array}$

We then search for subsets of these rules which entail at least one positive example and no negative examples:

 $f(List) \leftarrow f_3(List), f_4(List), f_5(List)$

3 - Theoretical Analysis

Theorem JOINER learns an optimal solution (a program with minimal size).

 Table 1: Predictive accuracies (%).

more than 100 literals.

Q3 JOINER can outperform existing approaches in terms of predictive accuracies.

5 - Conclusion and Limitation

An approach which learns big rules by joining small rules.
Future work: noisy examples.



